### **Dynamic Quantum Matter**

Dynamic 2: Dynamics in Dirac materials

• Dirac Materials

• Dynamics in Dirac Materials 1: Dynamic Exciton instability in DM

Dynamics in Dirac materials
2: Axial Magnetoelectric
Effect in DM

Conclusion







• Universal properties

- Scaling of DoS...
- Nontrivial topology
  - Surface states, anomaly, transport...
- Emergent gauge fields and geometry

bosonic analogues...

Wehling, Black-Schaffer, and Balatsky, Adv. Phys. 63, 1 (2014)

### Dirac equation

• Dirac equation (1928)

$$\begin{aligned} (i\gamma^{\mu}\partial_{\mu} - m)\psi &= 0 \\ \gamma^{\mu} &= \begin{bmatrix} 0 & \sigma^{\mu} \\ \bar{\sigma}^{\mu} & 0 \end{bmatrix}, \ \psi &= \begin{bmatrix} \psi_{L} \\ \psi_{R} \end{bmatrix} \\ \sigma^{\mu} &= (I, \boldsymbol{\sigma}), \ \bar{\sigma}^{\mu} &= (I, -\boldsymbol{\sigma}) \\ H_{\text{Dirac}} &= \begin{bmatrix} \boldsymbol{\sigma} \cdot \mathbf{k} & m \\ m & -\boldsymbol{\sigma} \cdot \mathbf{k} \end{bmatrix} \end{aligned}$$



### What is a Dirac material?

Dirac materials (DMs): low-energy fermionic excitations are described by a Dirac Hamiltonian

Dirac equation: 
$$i\hbar \frac{\partial}{\partial t}\psi = (\underline{c}\boldsymbol{\alpha} \cdot \mathbf{p} + \beta mc^2)\psi$$
  
 $\alpha = \begin{pmatrix} 0 & \sigma_i \\ \sigma_i & 0 \end{pmatrix}$   $\beta = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$ 
Dirac Hamiltonian:  $H_D = v_F \boldsymbol{\sigma} \cdot \boldsymbol{p}$   
in condensed matter  $v_F \approx c/300$ 



 $\mathbf{k}_{i}$ 

T.O. Wehling, A.M. Black-Schaffer, A.V. Balatsky, Advances in Physics (2014)

#### Dynamics examples:

#### Floquet approach



Gedik grp Nature Physics volume 12, pages 306–310 (2016)

#### Dynamic induction of superconductivity



Mitrano,M.*etal. Nature* **530,**461(2016). Kennes,D., et al, Nature Physics **14**, 1 (2017).

#### Driven Dirac Matter –

#### a platform for driven excitonic condensate



Collaboration with A Black-Schaffer, Bardarson, Bergholz, Bonetti, Tjernberg, Weissenrieder on dynamics of DM and STO

### Transient excitonic instability in optically pumped DM

- Exciton: a bound state of electron and hole
- Excitonic instability: exiton binding energy  $|E_B| > E_G \rightarrow$  ground state of an insulator becomes unstable  $\rightarrow$  collective state

Previous search for excitonic condensate:

- Spatially direct excitons (in semicond. or semimetal)
- Spatatially separated e-h systems:
  - semiconductor heterostructures [Lozovik, Yudson Zh. Eksp. Teor. Fiz. (1976)]
  - bilayer graphene [Eisenstein, MacDonald, Nat. Phys. (2004)]

Keldysh and Kopaev Sov. Phys.-Solid State (1965) Jerome, Rice, Kohn PR (1967); Halperin, Rice RMP(1968)







Many-body instability in driven DM

- Linear dispersion in  $DM \rightarrow vanishing DOS$  at the node
- Critical coupling for many-body instabilities
- Dirac nodes are stable against interactions
- Basic idea: move the states away from the node e.g. by pumping









A. Pertsova

C. Triola, A. Pertsova, A.V. Balatsky Physical Review B 95 (20), 205410 (2017) K Sumida, et al Scientific reports 7 (1),14080 (2017) A Pertsova, AV Balatsky Physical Review B 97 (7), 075109 (2018)

### Tunability of the critical coupling in a driven 2D Dirac material

Dimensionless coupling in DM:

$$\lambda \equiv \frac{E_C}{E_{kin}} = e^2 / \varepsilon \hbar v_F \rightarrow \text{critical } \lambda_c; \lambda_c \approx 1 \text{ in graphene}$$





Non-equilibrium drives a many-body instability



### Experimental feasibility

In pumped TIs bulk states are involved.

Sinding energy (eV) band (S Dirac poir 0.4 Bulk valence band (BVB) -0.05 0 0.05 k (1/Å) -0.1 0.1

21 eV 1.6 eV

G

Gigantic lifetime  $\tau \geq \mu s$ ? ٠





*t<0* 



t



*t<0* 

t=0



13

t











### Pumped Dirac Materials: Theory

- Excitonic instability can be realized in pumped 2D DM: excitonic gap ~ 10meV in valley-pumped graphene [Triola *et al.*, PRB 95, 205410 (2017) ]
- Here we study excitonic instability in pumped 3D DMs (Dirac and Weyl semimetals treated on equal footing)



### Excitonic phases in pumped 3D DM



# Dynamics of the order parameter

Semiconductor Bloch equations (SBE) for pumped 2D DM

occupations  $n_{k}^{e} = \left\langle a_{k}^{\dagger}a_{k} \right\rangle$   $n_{-k}^{h} = \left\langle b_{-k}^{\dagger}b_{-k} \right\rangle$   $f_{k} = \left\langle a_{k}^{\dagger}b_{-k}^{\dagger} \right\rangle$   $\Delta_{k}^{*} = -\sum V_{k-k'} \left\langle a_{k'}^{\dagger}b_{-k'}^{\dagger} \right\rangle$ interband polarization/cohérence

$$\begin{cases} \frac{dn_k^e}{dt} = i\Delta_k^* f_k^* - i\Delta_k f_k + \frac{dn_k^e}{dt}|_{scat}, \\ \frac{dn_{-k}^h}{dt} = i\Delta_k^* f_k^* - i\Delta_k f_k + \frac{dn_k^h}{dt}|_{scat}, \\ \frac{df_k}{dt} = i(\varepsilon_k^e + \varepsilon_k^h)f_k + i\Delta_k^*(1 - n_k^e - n_{-k}^h) + \frac{df_k}{dt}|_{scat} \end{cases}$$

 $\rightarrow$  dynamics of  $f_k(t)$ , order parameter  $\Delta(t)$ 

#### **Refs:**

Haug, Kohn, "Quantum theory of optical and electronic properties of semiconductors" Malic et al. PRB 84, 205406 (2011); Goldstein et al. PRB 91, 054517 (2015)



scattering terms:  $-\frac{n_k^e(t) - n_{\rm F}(\mu^e(t))}{T_1'}$  $n_k^e(t)$  $\frac{dt}{dt} |_{scat} =$ intraband relaxation interband relaxation (recombination)  $s_{cat} =$ dephasing  $(T \sim \Gamma^{-1})$  $1/T_2 = 1/T_1 + 1/T_1'$ 19

 $\frac{d\langle 0\rangle}{d} = i\langle [H, 0] \rangle + scat.$ 





# Dynamics of the order parameter

Lifetime of the transient excitonic state is controlled by the lifetime of the non-equilibrium e and h distributions.



Time-evolution of the gap  $\Delta_k$  and electron occupation  $n_k^e$  at  $k = k_F$ . Parameters for graphene with  $\alpha \approx 1$  and  $\mu = 200$  meV.

#### Experimental feasibility 3D DM (Dirac/Weyl)

#### Size of the gap and $T_c$ is controlled by:

- Coupling  $\alpha$
- Energy scale on which 3D Dirac cones exist ( $\Lambda$ )
- Dirac cone degeneracy

Estimates for a for a hypothetical 3D DM with different *g*, assuming cut-off energy scale of 1eV and single-valley pumping

| _ | System         | $\alpha$ | $\Lambda$ (eV) | $T_c$ (K) | $\Delta_{\rm max} \ ({\rm meV})$ |
|---|----------------|----------|----------------|-----------|----------------------------------|
|   | $Cd_3As_2 DSM$ | 0.1      | 1              | 0.1       | 0.03                             |
|   | TaAs WSM       | 1        | 0.2            | 2         | 0.3                              |
|   | 3D DM $g = 1$  | 1 - 3    | 1              | 1 - 20    | 0.3 - 3                          |
|   | 3D DM $g = 2$  | 1 - 3    | 1              | 10 - 60   | 1 - 10                           |
|   | 3D DM $q = 4$  | 1 - 3    | 1              | 1 - 2     | 0.1 - 0.3                        |

Large gaps (10meV) and  $T_{\rm c}$  (~100K) could be achieved in new materials.



C. Triola, A. Pertsova, A.V. Balatsky Physical Review B 95 (20), 205410 (2017)

K Sumida, et al Scientific reports 7 (1), 14080 (2017)

A Pertsova, AV Balatsky Physical Review B 97 (7), 075109 (2018)

Dynamically Induced Excitonic Instability in Pumped Dirac MaterialsA Pertsova, AV Balatsky Annalen der Physik 532 (2), 1900549 (2020) Possible X observation Y. Hou et al Nature Communications, 10, 5723 (2019). 10.1038/s41467-019-13711-3

### Emergence of excitonic superfluid at topological-insulator surfaces

Yasen Hou<sup>1</sup>, Rui Wang<sup>2</sup>, Rui Xiao<sup>1</sup>, Luke McClintock<sup>1</sup>, Henry Clark Travaglini<sup>1</sup>, John P. Francia<sup>1</sup>, Harry Fetsch<sup>3</sup>, Onur Erten<sup>4</sup>, Sergey Y. Savrasov<sup>1</sup>, Baigeng Wang<sup>5</sup>, Antonio Rossi<sup>1</sup> Inna Vishik<sup>1</sup>, Eli Rotenberg<sup>6</sup> & Dong Yu<sup>1\*</sup>



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Dynamic Multiferroic: Axial Magnetoelectric Effect



Floating Weyl nodes ~ axial gauge field Example: Sound generates magnetization in Cd3As2

Long Liang, P. O. Sukhachov, and A. V. Balatsky, arxiv dec 2020, PRL (2021)

# Dynamic in DM 2: Axial ME effect in Dirac materials

• Inverse Faraday effect IFE: photon torque -> dc M

 $M \sim E_{\omega} \wedge E_{\omega}^*$ 

- New Axial gauge fields in DM:  $H = \sigma(k \eta A_{5(r,t)})$   $\mathbf{E}_5 = -\partial_t A^5$
- Axial Magnetoelectric effect: axial gauge field (e.g. phonon) torque -> DC M

$$M \sim E_{\omega}^5 \wedge E_{\omega}^{*5}$$

Axial Magnetoelectric Effect in Dirac semimetals L Liang, PO Sukhachov, AV Balatsky, Phys. Rev. Lett. 126, 247202 (2021) arXiv:2012.07888

#### **Time-dependent**

#### $\langle A(t) \otimes B(t') \rangle \neq 0 - Dynamic MF -$



### Dirac equation

• Weyl fermions (1929)

$$egin{aligned} H_{ ext{Weyl}} = \left[egin{aligned} oldsymbol{\sigma} \cdot (\mathbf{k} - \mathbf{b}) + b_0 & 0 \ 0 & -oldsymbol{\sigma} \cdot (\mathbf{k} + \mathbf{b}) - b_0 \ (i\gamma^\mu \partial_\mu - egin{aligned} eta_\mu \gamma^\mu \gamma^5 )\psi = 0 \ \end{pmatrix} \end{aligned}$$

Positions of the Weyl points in energy-momentum space, axial 'gauge potential'

$$\mathbf{E}_5 = \partial_t \mathbf{b} - \nabla b_0$$

$$\mathbf{B}_5 = 
abla imes \mathbf{b}$$



### Dirac equation

• The Dirac equation is invariant under time reversal (T), inversion (I or P), and charge conjugation (C) symmetry





Peskin and Schroeder

- Current is odd under C, while axial current is even
- » Nonzero chemical potential breaks C

# Axial gauge fields in Dirac semimetals

• Space/time dependent Weyl nodes ~ axial gauge fields



Ilan, Grushin and Pikulin, Nat. Rev. Phys. 2, 29 (2020)

# Axial gauge fields in Dirac semimetals

• Manipulating Weyl nodes by light pulses



Light pulses induce structural changes in WTe<sub>2</sub> Sie et al., Nature **565**, 61 (2019)

# Inverse Faraday effect

• Heuristic explanation

$$m\ddot{\mathbf{r}} = -e\mathbf{E}(t) \quad \mathbf{E}(t) = E(\cos\omega t, \sin\omega t)$$



Static orbital magnetization  $\mathbf{M} \propto \mathbf{r} \times \dot{\mathbf{r}} \propto \frac{\mathbf{E}_{\omega} \times \mathbf{E}_{\omega}^*}{\omega^3}$ Dynamical multiferroicity  $\mathbf{M} \propto \mathbf{P} \times \partial_t \mathbf{P}$ Juraschek, Fechner, Balatsky, and Spaldin,

PRMaterials 1, 014401 (2017)

- Semiclassical theory, e.g., Pitaevskii, JETP 1960 Applies only to dissipationless materials
- Quantum theory, e.g., Battiato et al. PRB 2014, PRL 2016 Suitable for ab-initio calcualtions

### Inverse Faraday effect in Dirac semimetals





IFE in graphene, chemical is 0.2eV Tokman et al. PRB **101**, 174429 (2020) Topological IFE in magnetic Weyl semimetals Gao, Wang, and Xiao, arXiv: 2009.13392

### Inverse Faraday effect in Dirac semimetals





helicity dependent photocurrent in Bi-based Dirac semimetals Kawaguchi et al. arXiv: 2009.01388

## Magnetoelectric effect

• Coupling between electric and magnetic fields in matter

See e.g. Manfred Fiebig, J. Phys. D: Appl. Phys. **38** (2005) R123  $F(\vec{E}, \vec{H}) = F_0 - P_i^S E_i - M_i^S H_i$   $-\frac{1}{2} \epsilon_0 \epsilon_{ij} E_i E_j - \frac{1}{2} \mu_0 \mu_{ij} H_i H_j - \alpha_{ij} E_i H_j$   $-\frac{1}{2} \beta_{ijk} E_i H_j H_k - \frac{1}{2} \gamma_{ijk} H_i E_j E_k - \cdots$   $M_i(\vec{E}, \vec{H}) = M_i^S + \mu_0 \mu_{ij} H_j + \alpha_{ij} E_i$   $+ \beta_{ijk} E_i H_j + \frac{1}{2} \gamma_{ijk} E_j E_k - \cdots$ breaking
Linear magnetoelectric effect (ME) T and I breaking, topological ME in 3D topological insulators, Qi, Hughes, and Zhang, PRB, 2008

> Inverse Faraday effect, not forbidden by I and T T breaking by circularly polarized light,  $\mathbf{E} \times \mathbf{E}^*$ Proposed by Pitaevskii, JETP **12**, 1008 (1960)

### Axial magnetoelectric effect

$$M_i = \alpha_{5,ij} E_{5,j} + \beta_{5,ijk} E_{5,j} B_{5,j} + \frac{1}{2} \gamma_{5,ijk} E_{5,j} E_{5,k}$$

|   | $\mathbf{E}$ | Β  | $\mathbf{E}_5$ | $\mathbf{B}_5$ |
|---|--------------|----|----------------|----------------|
| Т | 1            | -1 | 1              | -1             |
| Ι | -1           | 1  | 1              | -1             |

### Axial magnetoelectric effect

$$\mathbf{M} = -\lim_{B \to 0} \frac{\partial \mathcal{S}_{\text{eff}}}{\partial \mathbf{B}}$$
$$e^{iS_{\text{eff}}} = \int \mathbf{D}\bar{\psi}\mathbf{D}\psi e^{i\int d^4x \mathcal{L}}, \ \mathcal{L} = \bar{\psi}(i\partial_{\mu} - A_{\mu} - A_{5,\mu}\gamma^5)\gamma^{\mu}\psi$$

SS m

$$S_{\rm eff} \sim \int \langle j^{\mu} j_{5}^{\nu} j_{5}^{\rho} \rangle A_{\mu} A_{5,\nu} A_{5,\rho} \qquad \begin{array}{c} j^{\mu} = \bar{\psi} \gamma^{\mu} \psi & \text{changes sign under C} \\ j_{5}^{\mu} = \bar{\psi} \gamma^{\mu} \gamma^{5} \psi & \text{unchanged under C} \end{array}$$



Triangle diagram, not to be confused with the diagrams giving the chiral anomaly

- Vanishes charge neutral point, Fermi surface effect
- Can be calculated separately for each node (IFE in the q=0 limit)
- Other effects such as photo/acoustogalvanic effect, Sukhachov and Rostami, PRL 2020

### Dirac semimetal Cd<sub>2</sub>As<sub>3</sub>



Z. K. Liu et al., Nat. Mater. **13**, 677 (2014) Large Fermi velocity, high mobility, long life time

### Axial magnetoelectric effect in strained Cd<sub>2</sub>As<sub>3</sub>

Transverse sound wave propagating in z direction

$$\mathbf{u} = \operatorname{Re} \left[ u_0 (\mathbf{e}_x - i\mathbf{e}_y) e^{i(q_z z - \omega t)} \right]$$
$$\mathbf{A}_5 = i(\mathbf{e}_x - i\mathbf{e}_y) \frac{b\beta u_0}{4e} q_z e^{i(q_z z - \omega t)} + \text{c.c.},$$

Transverse sound velocity  $v_s = 1.6 \times 10^3 \text{m/s}$ 

- Key differences between IFE and AME  $A_5 \propto q_z \propto \omega, E_5 \propto \omega^2$ 

 $\omega \ll v_F q_z$  : momentum dependence can't be ignored

# Axial magnetoelectric effect in strained Cd<sub>2</sub>As<sub>3</sub>



μ is fixed to be 0.2eV (μτ~3 for τ=0.01ps) For τ=1ps and ω=1GHz, μ<sub>0</sub>M<sub>z</sub>≈1μG

 $q_z v_z \tau \ll 1 \text{ limit}$   $M_z \approx M_0 \left[ 1 - \frac{3}{5} (q_z v_z \tau)^2 \right] \mu \omega \tau^2 \propto \omega$   $q_z v_z \tau \gg 1 \text{ limit}$   $M_z \approx 3M_0 \frac{1}{(q_z v_z \tau)^2} \left[ 1 - \frac{\pi}{2(q_z v_z \tau)} \right] \mu \omega \tau^2 \propto 1/\omega$   $M_0 = \frac{e v_x v_y (\beta b u_0 q_z)^2}{48\pi^2 v_z} \propto I$ 

 $I=10W/cm^2$  is the sound intensity,  $u_0=0.2nm$  when  $\omega=1GHz$ 

# Axial magnetoelectric effect in strained Cd<sub>2</sub>As<sub>3</sub>

 $\times 10^{-7}$ 2  $\mu_0 M_z$ (Gauss) 1.5 1 0.5 10 8 0 80 6 60 40  $\mu(\text{meV})$ 20 2 0  $\omega(\text{GHz})$ 

т=1ps

|     | small $\omega$     | large $\omega$       |  |
|-----|--------------------|----------------------|--|
| IFE | $\propto 1/\omega$ | $\propto 1/\omega^3$ |  |
| AME | $\propto \omega$   | $\propto 1/\omega$   |  |

Two peaks at  $\omega \tau \propto v_x / v_z, \ q_z v_z = 2\mu$ 

# Conclusion Dynamic 2

- Nodal states due to topology- new ground to probe dynamics
- Proposed transient exciton instability in DM
- Axial Magnetoelectric effect time dependent synthetic gauge fieds in nodal material
- Effect is on the scale of
- Dynamic 3: Dark Matter Dynamics and Quantum Sensors